



# ESSLI Summerschool 2014: Intro to Compositional Semantics

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Fifth Lecture: Propositions and Intensions

Intensional  
Contexts

Cases and  
Proposi-  
tions

Logical  
Space

From  
Proposi-  
tions to  
Intensions

Composing  
Intensions

Hintikka's  
Attitudes



[from Lecture 2]

## LOGICAL [or FORMAL] SEMANTICS

The **meaning** of any expressions has (at least) **two components**, viz. its:

- **intension**  $\approx$  its contribution to the content of expressions in which it occurs
- **extension**:  $\approx$  its contribution to the reference of expressions in which it occurs
- ... and maybe more (but not in this course)

In the simplest cases:

- Intension is content.
- Extension is reference.



- (1) a. Pfäffingen is larger than Breitenholz
- b. Hamburg is larger than Cologne
- c. John knows that Pfäffingen is larger than Breitenholz
- d. John knows that Hamburg is larger than Cologne
  
- (2) a. There are no thieves
- b. There are no murderers
- c. John is an alleged thief
- d. John is an alleged murderer
- e. The criminologist is looking for a thief
- f. The criminologist is looking for a murderer



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- (3) Four fair coins are tossed
- (4) At least one of the 4 tossed coins lands heads up
- (5) At least one of the 4 tossed coins lands heads down
- (6) Exactly 2 of the 4 tossed coins land heads up
- (7) Exactly 2 of the 4 tossed coins land heads down



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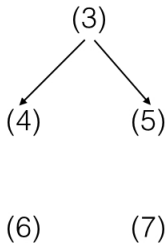
(3)

(4)            (5)

(6)            (7)

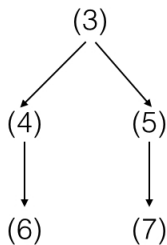


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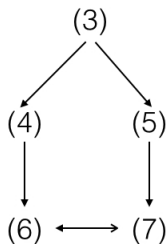


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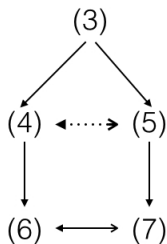
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- (8) John knows that at least one of the 4 tossed coins lands heads up
- (9) John knows that at least one of the 4 tossed coins lands heads down
- (10) *Most Certain Principle*  
If a (declarative) sentence  $S_1$  is true and another sentence  $S_2$  is false in the same circumstances, then  $S_1$  and  $S_2$  differ in meaning.
- (11) John knows that exactly two of the 4 tossed coins lands heads up
- (12) John knows that exactly two of the 4 tossed coins lands heads down
- (13) *Definition [to be revised]*  
The **proposition** expressed by a sentence is the set of possible cases of which that sentence is true.



(14)

possible cases	$C_1$	$C_2$	$C_3$	$C_4$
1	1	1	1	1
2	1	1	1	0
3	1	1	0	1
...	...	...	...	...
14	0	0	1	0
15	0	0	0	1
16	0	0	0	0

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- (15) a. Four coins were tossed when John coughed  
b. Four coins were tossed and no one coughed

(16) *[Revised] Definition*

The **proposition** expressed by a sentence is the set of possible worlds of which that sentence is true.

(17) *Definition*

A sentence  $S$  is **true of** [or **at**] a possible world  $w$  if and only if  $\llbracket S \rrbracket_w = 1$ .

(18) By  $\llbracket S \rrbracket$  we mean the proposition expressed by  $S$ :

$$\llbracket S \rrbracket := \{ w : \llbracket S \rrbracket_w = 1 \}$$

(19) A sentence  $S$  is true of a possible world  $w$  if and only if  $w \in \llbracket S \rrbracket$ .

(20)  $\llbracket S \rrbracket_w = 1$  iff  $w \in \llbracket S \rrbracket$ .



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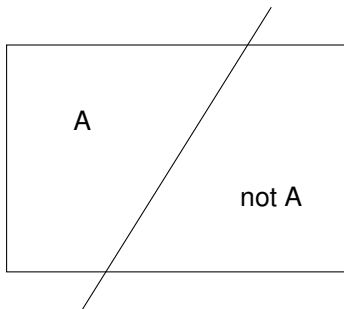
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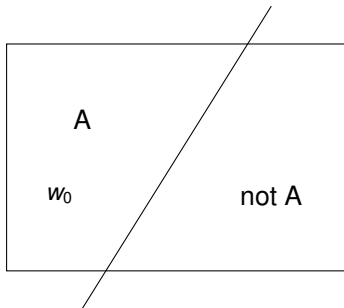
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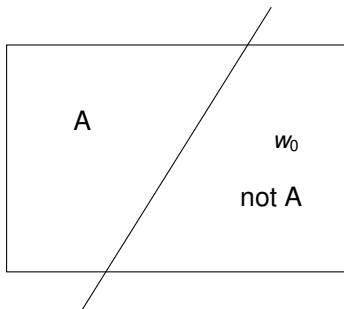
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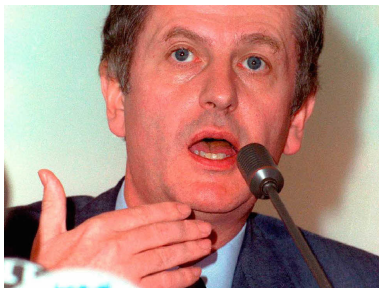
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## (21) Barschel was murdered<sup>1</sup>



<sup>1</sup>Uwe Barschel [1944–1987] was a German politician who had to resign as the prime minister of Schleswig-Holstein under scandalous circumstances (comparable to the Watergate affair) and who was found dead in the bathtub of his hotel room a few days after his resignation. The circumstances of his death could never be fully clarified.





(22)

world	truth value
$w_1$	1
$w_2$	0
$w_3$	1
...	...
$w_n$	0
...	...

(23) *Definition*

The **intension** of  $\alpha$ , written as  $\llbracket \alpha \rrbracket$ , is that function  $f$  such that for every possible world  $w$ ,  $f(w) = \llbracket \alpha \rrbracket_w$ .



(24) *Principle of Intensional Compositionality*

The intension of a complex expression is a function of the intensions of its immediate parts and the way they are composed.

EXTENSIONAL CONSTRUCTIONS:

(25) For any world  $w$ :

$$\begin{aligned} & \llbracket \text{Paul is sleeping} \rrbracket (w) \\ = & \llbracket \text{Paul is sleeping} \rrbracket_w \\ = & \llbracket \text{Paul} \rrbracket_w * \llbracket \text{is sleeping} \rrbracket_w \\ = & \llbracket \text{Paul} \rrbracket (w) * \llbracket \text{is sleeping} \rrbracket (w) \end{aligned}$$



## INTENSIONAL CONSTRUCTIONS

- (26) a. John knows that [ Hamburg is larger than Cologne ]  
b. John knows that [ Pfäffingen is larger than Breitenholz ]

$$(27) \quad \llbracket \textit{John knows that S} \rrbracket_w = 1 \text{ iff } \langle \llbracket \textit{John} \rrbracket_w, \llbracket \textit{S} \rrbracket \rangle \in \llbracket \textit{know} \rrbracket_w$$

$$(28) \quad \text{For any world } w:$$
$$= \llbracket \textit{attitude verb + that + S} \rrbracket_w$$
$$= \llbracket \textit{attitude verb} \rrbracket_w \overset{*}{\rightarrow} \llbracket \textit{S} \rrbracket$$
$$= \llbracket \textit{attitude verb} \rrbracket (w) \overset{*}{\rightarrow} \llbracket \textit{S} \rrbracket$$



## INTENSIONAL CONSTRUCTIONS

(29) John is an alleged thief / murderer

(30) For any world  $w$ :  
[[ intensional-adjective + noun ]] <sub>$w$</sub>   
= [[ intensional-adjective ]] <sub>$w$</sub>  ( [[ noun ] ] )

(31) The criminologist is looking for a thief / murderer

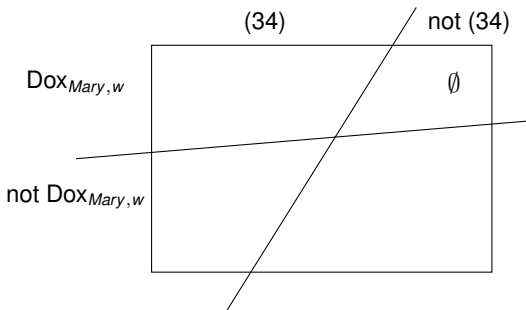
(32) For any world  $w$ :  
[[ opaque verb + quantifier phrase ]] <sub>$w$</sub>   
= [[ opaque verb ]] <sub>$w$</sub>   $\xrightarrow{*}$  [[ quantifier phrase ]]



(33) Mary thinks that John is in Rome

(34) John is in Rome

(35)





$$(36) \quad \llbracket \text{think} \rrbracket_w = \{ \langle x, p \rangle : \text{Dox}_{x,w} \subseteq p \}$$

$$(37) \quad \llbracket \text{know} \rrbracket_w = \{ \langle x, p \rangle : \text{Epi}_{x,w} \subseteq p \}$$

$$(38) \quad \llbracket \text{want} \rrbracket_w = \{ \langle x, p \rangle : \text{Bou}_{x,w} \subseteq p \}$$

(39) Mary knows that Bill snores  
 $\models$  Mary thinks that Bill snores

$$(40) \text{ a. } \text{Epi}_{\text{Mary},w} \subseteq \llbracket \text{Bill snores} \rrbracket$$

$$\text{ b. } \text{Dox}_{\text{Mary},w} \subseteq \llbracket \text{Bill snores} \rrbracket$$

$$(41) \quad \text{Dox}_{x,w} \subseteq p \text{ whenever } \text{Epi}_{x,w} \subseteq p.$$

$$(42) \quad \text{Dox}_{x,w} \subseteq \text{Epi}_{x,w}$$



(43) Mary knows that Bill snores

⊨ Bill snores

(44) #Mary knows that Bill snores, but Bill doesn't snore

[Cf.: Mary believes that Bill snores, but (in fact) Bill doesn't snore ]

(45)  $w \in \text{Epi}_{x,w}$

(46) Mary doesn't know that Bill snores

⊨ Bill snores

(47) Mary thinks that Bill has two or three children

⊨ Mary thinks that the number of Bill's children is prime